Magnetic ordering and spin reorientation in ErGa₃

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Calorimetric measurements between 0.3 and 10 K have been made on a single crystal of the AuCu₃-type cubic compound ErGa₃. The temperature dependence of specific heat exhibits an antiferromagnetic orderinginduced peak near 2.7 K, a second peak at 2.5 K due to spin reorientation, and a Schottky anomaly with crystal-field parameters x=0.17 and W=0.22 K, all in agreement with the results from neutron studies. The sum of the calculated entropies associated with the order-disorder process (*R* ln 2) and the crystal-field effect, respectively, is lower by 0.1*R* than the experimentally derived magnetic entropy values at approximately 6–10 K. This difference provides an estimate of a 2-J/mol latent heat for the spin rotation process. An anticipated transition from an amplitude-modulated magnetic structure to an equal magnetic-moment structure at temperatures near $T_N/2$ was not observed.

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Rare-earth-based compounds often undergo magnetic ordering, some of them followed by spin reorientation at lower temperatures. Among the different experimental techniques, calorimetric measurements play a unique role in providing thermodynamic quantities including energy and entropy associated with these processes. In a recent paper¹ on Er_3Ge_4 , a specific-heat peak at 7 K and a second one at 3.5 K confirmed the antiferromagnetic ordering and a spin reorientation, respectively, suggested by neutron diffraction. A sizable latent heat was obtained for the second transition. This report describes a similar work from 10 down to 0.3 K on another Er-intermetallic ErGa₃. An antiferromagnetic transition in this compound was first identified by Morin et al.² More extensive dc magnetization and neutron-diffraction studies by Murasik et al.3,4 indicated that the ordering at the Néel temperature $T_N = 2.83$ K occurred through a continuous transition and the magnetic structure appeared to be an incommensurate sinusoidally modulated one. Furthermore, they revealed two successive spin reorientations in zero applied field at $T_1 = 2.6$ K and T_2 in the vicinity of T_N , respectively. With lowering temperature one may expect the amplitudemodulated structure to evolve or transit toward an equal moment structure, of an antiphase type if it remains incommensurate or simple commensurate.

ErGa₃ single crystals were grown by the molten-metal solution method. The melt of composition of 90-at. % Ga (6*N*) and 10-at. % Er (3*N*) was slowly cooled from 920 °C to 350 °C at the rate of 0.8 °C/h before a rapid cooling to avoid the formation of ErGa₆ in a peritectic reaction. This procedure yielded single crystals of stoichiometric ErGa₃ immersed in an excess of pure gallium, which was easily removed. The high quality of the crystals was confirmed by x-ray diffraction showing the expected cubic AuCu₃-type structure. Complemented by ac susceptometry, calorimetric

measurements were made using a thermal-relaxation approach. A milligram-size specimen was thermally anchored with a minute amount of grease to a sapphire holder, which had a Cernox temperature sensor and a nickel-chromium alloy film as the Joule-heating element. The holder was linked thermally to a copper block by four Au-Cu alloy wires. The temperature of the block could be raised in steps but held constant when a heat pulse was applied to the specimen. Following each heat pulse, the specimen temperature relaxation rate was monitored to yield a time constant τ . Heat capacity was then calculated from the expression $c = \kappa \tau$, where κ is the thermal conductance of the Au-Cu wires. The heat capacity of the specimen holder was measured separately for addenda correction. The specific heat of the specimen was then obtained from $C = (c - c_{addenda})/(m/M)$ with m and M being the specimen mass and the molar mass of ErGa₃ (376.42 g/mol), respectively.

Figure 1 presents the temperature dependence of the specific heat of ErGa₃. Also shown are the data for an isostructural but nonmagnetic reference compound LuGa₃, which were obtained using a quasiadiabatic heat-pulse technique in Wroclaw. There are two maxima for ErGa₃, more clearly in the inset, at 2.5 and 2.7 K, respectively. The highertemperature peak is believed to be associated with the antiferromagnetic ordering, even though 2.7 K is lower than the Néel temperature $T_N = 2.83$ K as determined from magneticsusceptibility measurements.³ Such a phenomenon may be expected in systems with incommensurate amplitudemodulated magnetic structures when contribution of higher harmonics to the order parameter is large enough.⁵ The peak at 2.5 K undoubtedly corresponds to the afore-mentioned T_1 , arising from an abrupt reorientation of Er^{3+} spins from nearly the $\langle 110 \rangle$ direction towards the $\langle 100 \rangle$ axis.³ However, judging from the calorimetric data below 2.5-0.3 K, there is



FIG. 1. Temperature dependence of specific heat of $\text{ErGa}_3(+)$ and the nonmagnetic reference compound LuGa₃ (solid curve). Also shown for ErGa_3 are the magnetic contribution (\bigcirc), $C(m) = C - C(\text{LuGa}_3)$, and the calculated Schottky contribution (dashed curve) for comparison. Inset: Expanded plot revealing two peaks at 2.5 and 2.7 K, respectively.

no observable anomaly near $T_N/2$. It indicates that the squaring of the amplitude-modulated magnetic structure of ErGa₃ goes through an evolution of higher-order harmonics of the order parameter.⁶

The magnitude of the spin rotation effect in Fig. 1 is relatively small as compared to that in Er_3Ge_4 .¹ It is understandable, realizing that the complex magnetic behavior of orthorhombic Er_3Ge_4 arises from the intrinsic magnetic frustration caused by two nonequivalent Er^{3+} sites. In contrast, cubic ErGa_3 has a much higher structural symmetry, and the transition at T_1 involves only a relatively minor moment tilting. It is not surprised then that the other transition at T_2 near T_N has no distinguishable effect on specific heat.

In analyzing the calorimetric data, the total specific heat needs first to be delineated into its lattice, electronic, and magnetic contributions:

$$C = C(l) + C(e) + C(m).$$
 (1)

This is done by assuming that the lattice plus electronic contributions are equal to the specific heat of nonmagnetic LuGa₃ ($\gamma = 6.7$, $\beta = 0.47$ mJ/mol K⁴ with a corresponding $\theta_D = 161$ K). The magnetic contribution C(m) = C $-C(LuGa_3)$ is then calculated and shown as a function of temperature in Fig. 1. It actually contains three components:

$$C(m) = C_{\text{O-D}} + C_{\text{sr}} + C_{\text{Sch}}.$$
 (2)

 $C_{\text{O-D}}$ and C_{sr} are associated with the order-disorder (O-D) process and the spin rotation, respectively, whereas C_{Sch} is a Schottky term originating from the crystal-field (CF) splitting of the ${}^{4}\text{I}_{15/2}$ multiplet of Er^{3+} ions. $C_{\text{O-D}}$ and C_{sr} dominate C(m) below T_{N} . The short-range-ordering contribution persists to almost 6 K. In general, one does not have an easy handle on critical phenomena, but the paramagnetic behavior of C_{Sch} can be determined from

$$C_{\rm Sch}/R = (\langle E^2 \rangle - \langle E \rangle^2)/k_B^2 T^2, \qquad (3)$$

where R and k_B are the gas constant and Boltzmann's constant, respectively, and a statistical average over the CF levels with energy E_i is defined as

$$\langle x \rangle = \frac{\sum_{i=1}^{n} x_i \exp(-E_i/k_B T)}{\sum_{i=1}^{n} \exp(-E_i/k_B T)}.$$
(4)

Accordingly, the experimental data of $C_{\text{Sch}} \cong C(m)$ between approximately 6 and 10 K are reasonably well fitted by CF parameters x = 0.17 and W = 0.22 K, following the scheme of Lea, Leask, and Wolf.⁷ These parameters give a doublet Γ_7 as the ground state, a quartet $\Gamma_8^{(1)}$ at 28 K as the first-excited level, and an overall CF splitting equal to 110 K. They agree very well with parameters x = 0.19 and W = 0.25 K determined directly by inelastic neutron scattering.⁴

It is possible to obtain a reasonable estimate of the latent heat associated with the spin rotation from entropy consideration. Figure 2(a) shows a plot of C(m)/T versus *T*, from which the magnetic entropy is derived from

$$S(m) = \int \left[C(m)/T \right] dT$$
(5)

and presented in Fig. 2(b). Following Eq. (2), S(m) also consists of three components:

$$S(m) = S_{\text{O-D}} + S_{\text{sr}} + S_{\text{Sch}} = \int (C_{\text{O-D}}/T)dT + \int (C_{\text{sr}}/T)dT + \int (C_{\text{sr}}/T)dT + \int (C_{\text{Sch}}/T)dT.$$
(6)

While the exact determination of $C_{\text{O-D}}$ and C_{sr} is difficult, one has nevertheless a maximum value of $S_{\text{O-D}}=R \ln 2$ or $S_{\text{O-D}}/R=0.693$ for the ground-state doublet of Er^{3+} ions. At



FIG. 2. (a) C(m)/T versus *T* as basis for entropy calculations. (b) Temperature dependence of magnetic entropy. Note the $S_{\rm sr}$ -caused parallel difference above ~6 K between the experimental data (\bullet) and the solid line, which represents the sum of *R* ln 2 for $S_{\rm O-D}$ and $S_{\rm Sch}$ (dashed line) associated with the CF splitting.

a first look, the experimental value of S(m)/R in Fig. 2(b) is indeed close to 0.7 at T_N . However, the maximum $S_{\text{O-D}}$ value would not be achieved until all short-range ordering beyond T_N vanishes. Judging from Fig. 1, this needs to reach somewhere close to 6 K. Consequently, the seemingly coincidental observation of $S(m)/R \cong \ln 2$ at T_N gives a clear signal of the S_{sr} contribution below T_N , where S_{Sch} is negligible.

Finally, if the spin rotation were absent, the expected S(m) between approximately 6 and 10 K should follow the solid line in Fig. 2(b), which represents simply the sum of $R \ln 2$ and S_{Sch} as calculated from the calorimetrically determined crystal-field parameters. Instead, the actually observed S(m) values are higher by a roughly temperature independent 0.1R, a quantity now assigned to S_{sr} . Since this spin rotation occurs near 2.5 K, $S_{\text{sr}} \approx 0.1R = 0.83$ J/mol K would

lead to a small latent heat of the order of 2 J/mol. In comparison, it is 30 or 10 J/mol Er in Er_3Ge_4 .

In conclusion, calorimetric data of $ErGa_3$ support the findings from magnetic and neutron studies on magnetic transitions at T_N and T_1 , with additional information in terms of the associated entropy and latent heat. No indication of an additional phase transition at $T_N/2$ is observed in the presented data, contrary to the expectations. The anticipated transition near $T_N/2$ is from the amplitude-modulated magnetic structure to an equal magnetic-moment structure. Most likely, with the temperature lowering this structure evolves to an antiphase one through growing of higher-order harmonics in the order parameter.

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